

# Final Review

CMPUT 397

Fall 2020

# Comments: Dec 4

- The Final will be of the same format as the Midterm
  - on eClass, with long answer questions
  - 2 hours to complete the exam
- Practice Finals have been released

# Reviewing the Entire Course

- We recently reviewed Course 1 and Course 2
- To review Course 3, we primarily ask: how are things different under function approximation?

# How are things the same?

- We were always try to estimate a function:  $v_\pi$  or  $q_\pi$  or  $v^*$  or  $q^*$  or  $\pi$  itself
- $v_\pi : \mathcal{S} \rightarrow \mathbb{R}$ ,  $q_\pi : \mathcal{S} \times \mathcal{A} \rightarrow \mathbb{R}$  and so on
- The main difference is in the type of function we learn to try to get an accurate estimate of these true functions

# How are things different?

- Before, we were able to represent this function exactly, with a table (tabular)
  - $V$  is a vector (or array) of size number of states, with entry  $V(s)$  estimating  $v_{\pi}(s)$
- More generally, we can only approximate these functions
  - e.g.,  $\hat{v}(s, w) \approx v_{\pi}(s)$  for each  $s$ , for parameterized function  $\hat{v}(\cdot, w)$
- Tabular is a special case:  $V(s) = \hat{v}(s, w)$  under tabular features ( $x(s)$  one-hot encoding)
- Can also see it as a generalization, rather than a difference

# What is the source of inaccuracy?

- For tabular estimate  $V$ , the inaccuracy is due to insufficient samples and/or updates
  - Question: when and why is  $V$  inaccurate in DP? Do we eventually converge to  $v_\pi$ ?
  - Question: when and why is  $V$  inaccurate in TD? Do we eventually converge to  $v_\pi$ ?
- For more general parameterized functions,  $\hat{v}(\cdot, w)$ , the inaccuracy is due also to the inability to represent  $v_\pi$

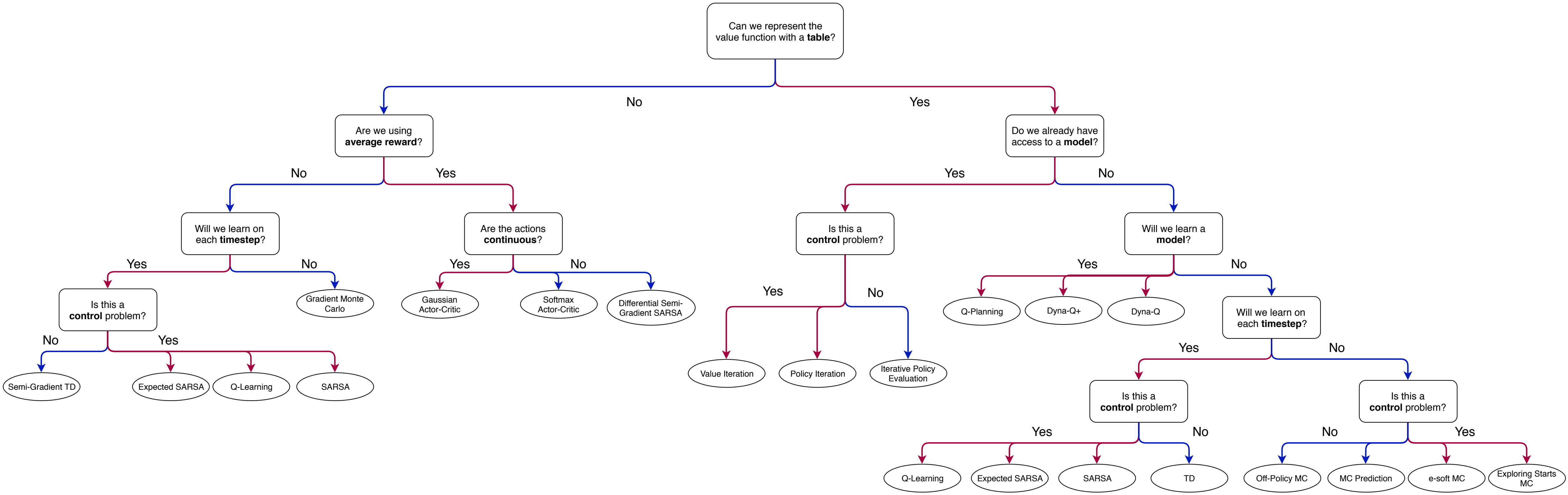
# Inaccuracy under FA

- All algorithms (tabular and more general parameterized functions) initialize the weights  $w$  to some value
- $\hat{v}(\cdot, w)$  is inaccurate after 10 updates because it has not seen enough samples
  - just like in the tabular setting
- In the limit of samples and updates,  $\hat{v}(\cdot, w)$  might still be inaccurate
  - even for  $w^*$ , the best weights we could obtain under infinite data and samples, we might have that  $\hat{v}(s, w^*) \neq v_\pi(s)$

# Estimation error and Approximation error

- $\hat{v}(\cdot, w)$  is inaccurate after 10 updates because it has not seen enough samples
  - this is called **estimation error** (due to insufficient data)
- In the limit of samples and updates,  $\hat{v}(\cdot, w)$  might still be inaccurate
  - this is called **approximation error** (also called the bias of the estimator)

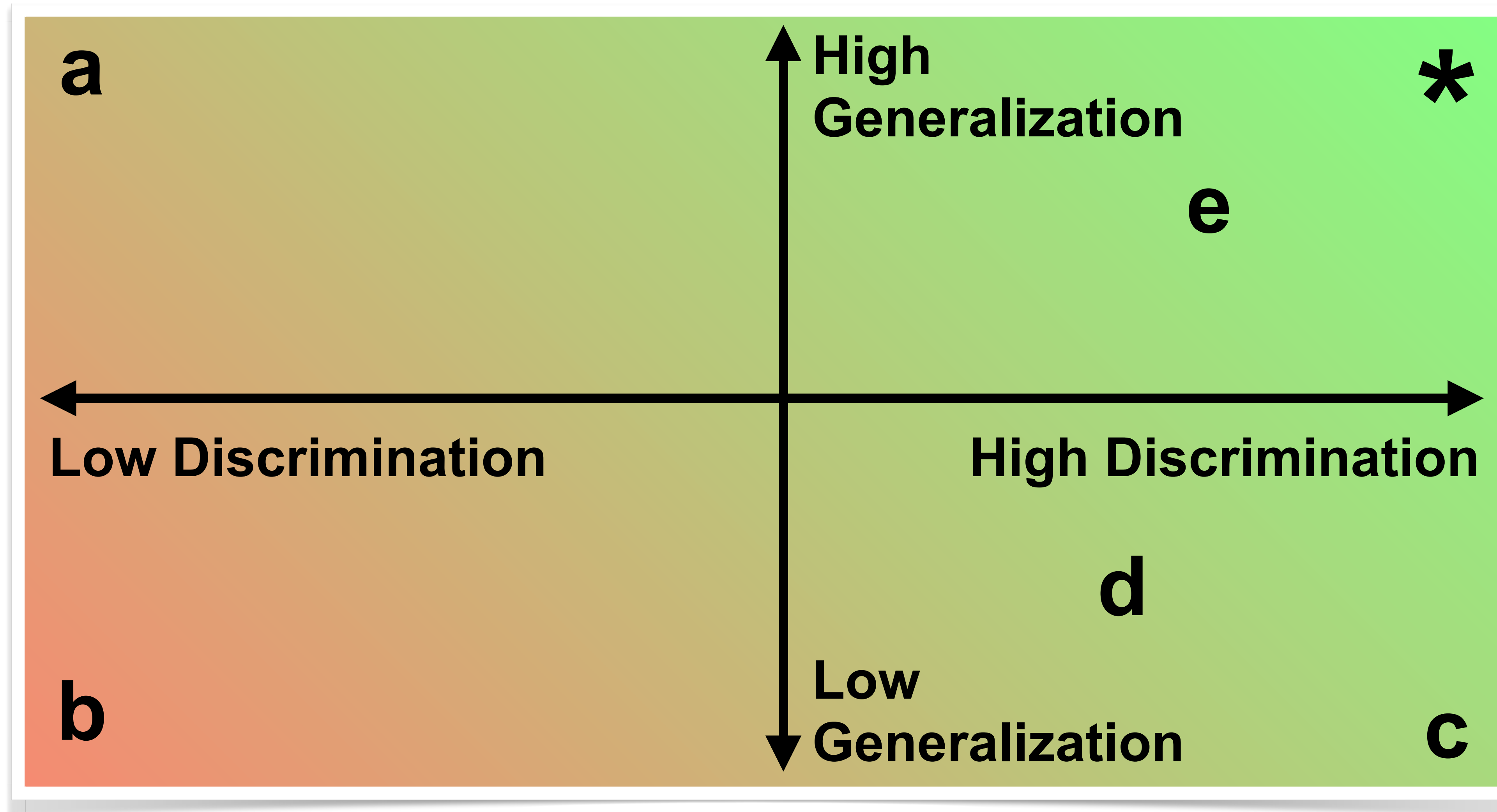




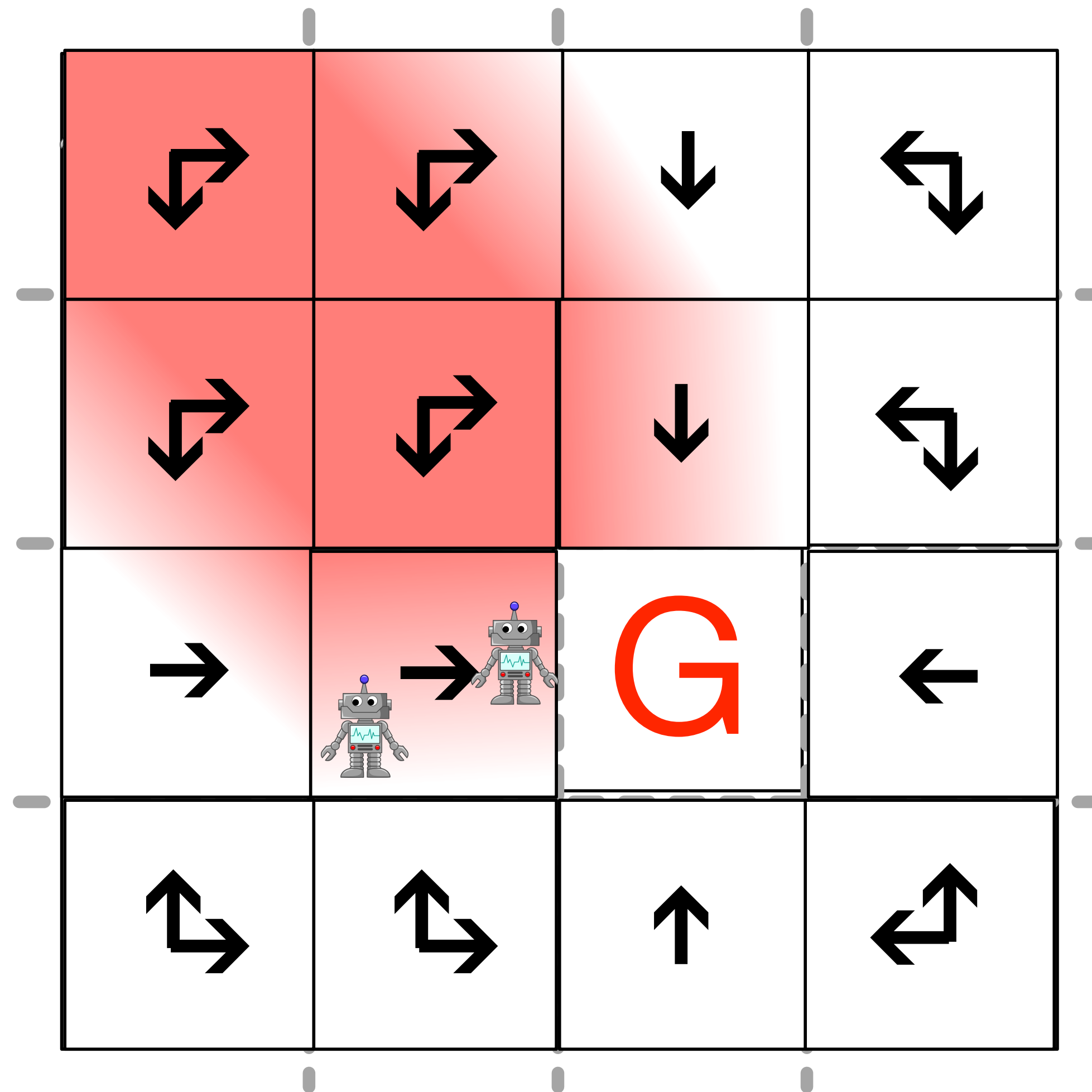
# Self-test: How would we use FA for bandits?

- When we did bandits, we estimated  $Q(a)$
- What might you use for  $\hat{q}(a, w)$ ? First, what is the tabular form, to represent  $Q(a)$ ?
- Now imagine I tell you there are 1000 actions, and actions 1 - 20 are similar, 21-25 are similar, 25-40 are similar and 40-1000 are similar. What features might you use?
- Is this FA better than the tabular one? Why or why not?

# Generalization and Discrimination



# Due to approximation error from FA we need a way to decide trade-offs in error across states

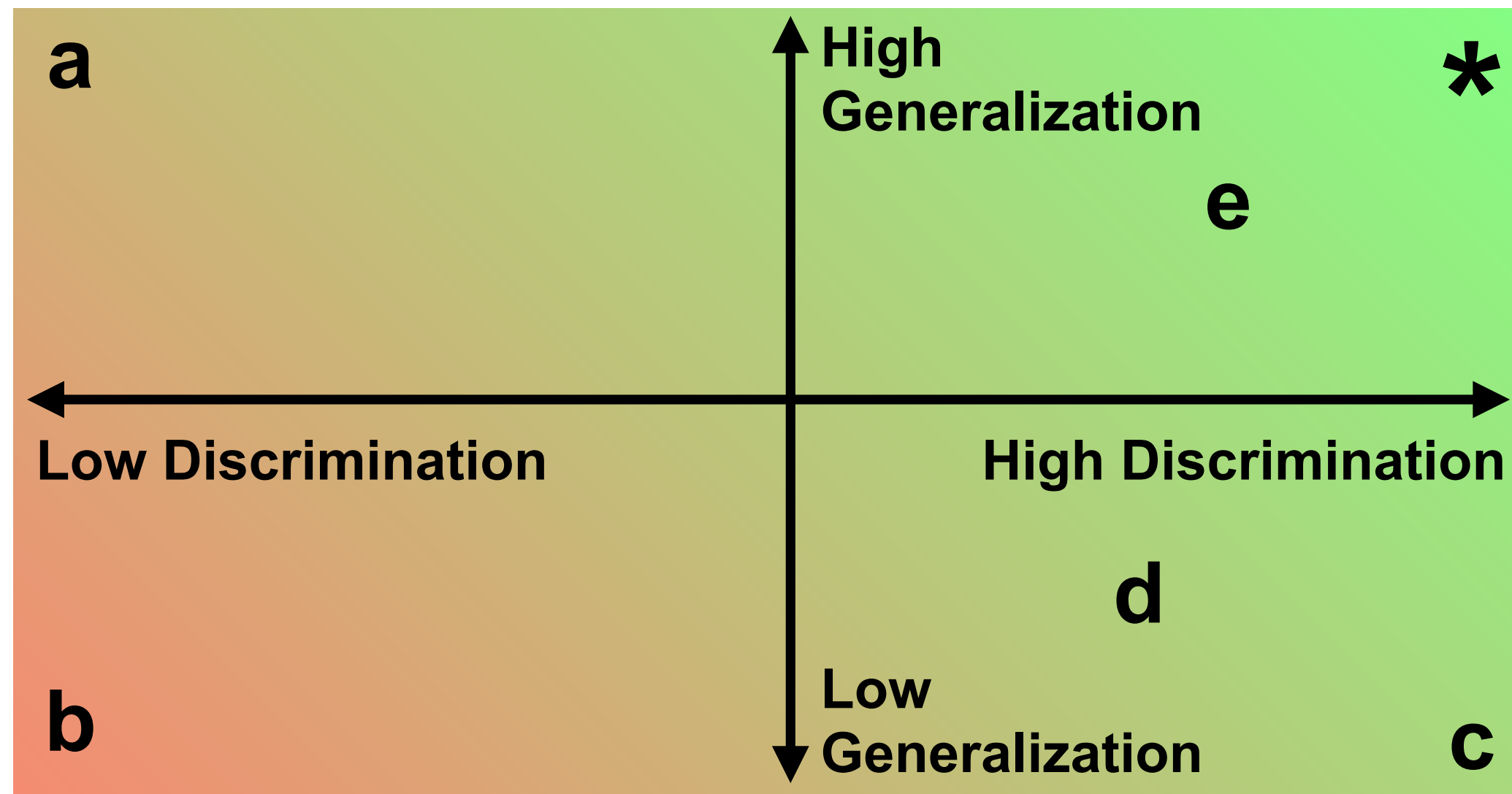


**Mean Squared  
Value Error**

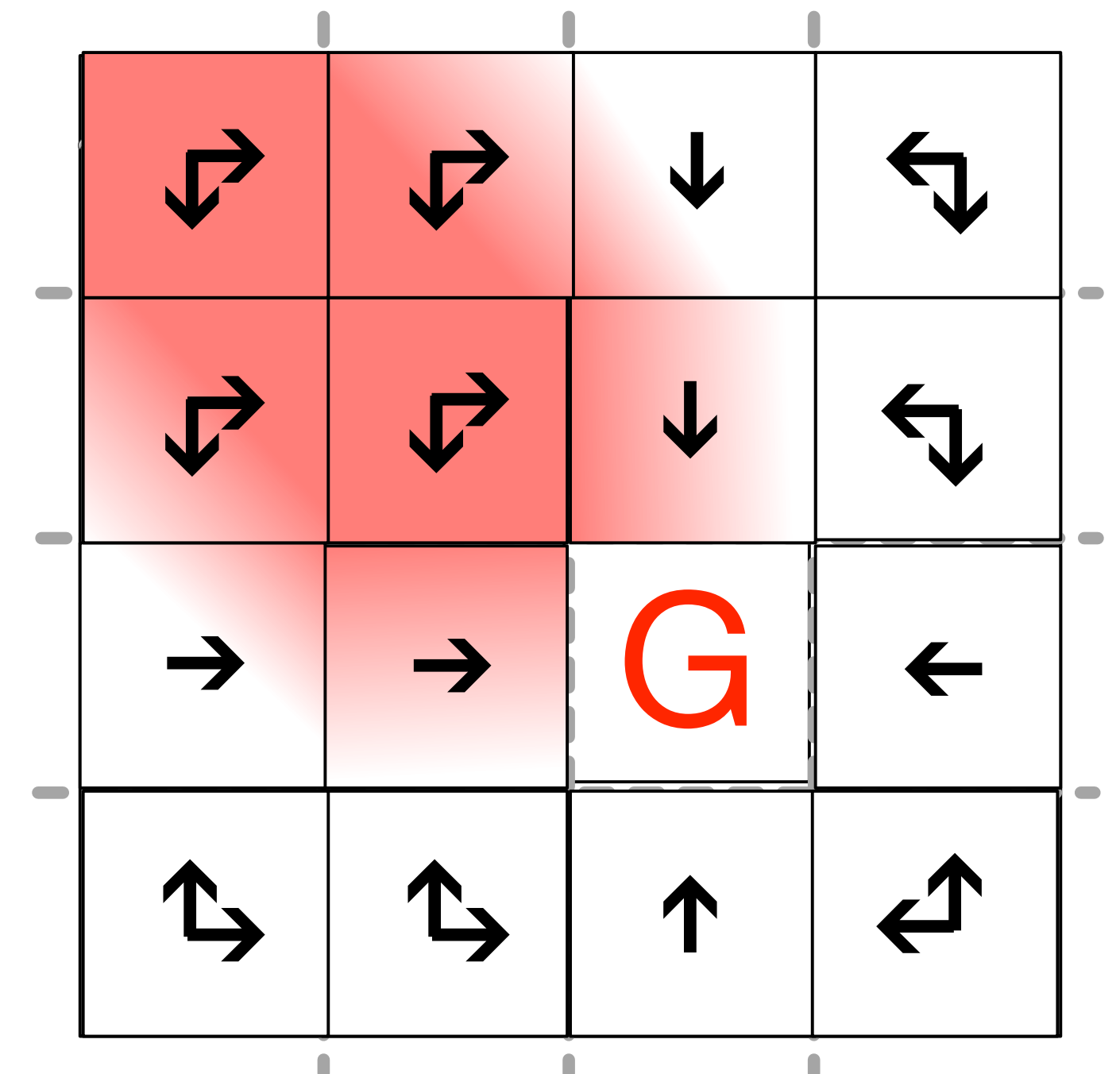
$$\sum_s \mu(s) [v_\pi(s) - \hat{v}(s, \mathbf{w})]^2$$

**The fraction of  
time we spend in  $S$   
when following  
policy  $\pi$**

# Self-test: How does the FA and the Weighting $\mu$ in the VE interact?



$$\sum_s \mu(s) [v_\pi(s) - \hat{v}(s, \mathbf{w})]^2$$



Question 1: Imagine we have features that correspond to a. Will what be accurate?  
If no, where will it be more inaccurate and where will it be more accurate?

Question 2: How about e? And how about at the star?

# Let's go through some quiz questions

- C3M1: Q5, Q8, Q9, Q10, Q11
- C3M2: Q3, Q5, Q9, Q11
- C3M3: Q1, Q2, Q8
- Final comment: The final will only include concepts from Course 1, 2 and 3, and will not include anything about average reward and importance sampling.
- You will not be tested on guest lectures, nor on content in Course 4