Course 1, Module 5 Dynamic Programming CMPUT 397 Fall 2019

Admin: Oct 4, 2019

- If you are auditing: send me an email and I can add you to eclass
- A proposed modification: discussion question due on Tuesday, rather than Sunday
 - more mental load for you, since multiple days where you have to submit
 - but, gives you more time to ask a meaningful question

Questions 1 and 2

generate a sequence of action value functions q_k ?

$$v_{k+1}(s) = \sum_{a} \pi(a|s) \sum_{s',r} p(s',r|s,a) \left[r + \gamma v_k(s')\right]$$

1. In iterative policy evaluation, we seek to find the value function for a policy π by applying the Bellman equation many times to generate a sequence of value functions v_k that will eventually converge to the true value function v_{π} . How can we modify the update below to

2. A deterministic policy $\pi(s)$ outputs an action $a \in \mathcal{A} = \{a_1, a_2, \ldots, a_k\}$ directly. More generally, a policy $\pi(\cdot|s)$ outputs the probabilities for all actions: $\pi(\cdot|s) = [\pi(a_1|s), \pi(a_2|s), \dots, \pi(a_k|s)]$. How can you write a deterministic policy in this form? Let $\pi(s) = a_i$ and define $\pi(\cdot|s)$.





Challenge Question 2

The policy iteration algorithm on page 80 has a subtle bug in that it may never terminate if the policy continually switches between two or more policies that are equally good. This is ok for pedagogy, but not for actual use. Modify the pseudocode so that convergence is guaranteed. Note that there is more than one approach to solve this problem.

- 1. Initialization
- 2. Policy Evaluation Loop:
 - $\Delta \leftarrow 0$ $v \leftarrow V(s)$

until $\Delta < \theta$ (a small positive number determining the accuracy of estimation)

3. Policy Improvement policy-stable $\leftarrow true$ For each $s \in S$: old-action $\leftarrow \pi(s)$

Policy Iteration (using iterative policy evaluation) for estimating $\pi \approx \pi_*$

 $V(s) \in \mathbb{R}$ and $\pi(s) \in \mathcal{A}(s)$ arbitrarily for all $s \in S$

Loop for each $s \in S$: $V(s) \leftarrow \sum_{s',r} p(s',r|s,\pi(s)) \left[r + \gamma V(s')\right]$ $\Delta \leftarrow \max(\Delta, |v - V(s)|)$

 $\pi(s) \leftarrow \operatorname{arg\,max}_{a} \sum_{s',r} p(s',r|s,a) [r+\gamma V(s')]$ If old-action $\neq \pi(s)$, then policy-stable \leftarrow false If *policy-stable*, then stop and return $V \approx v_*$ and $\pi \approx \pi_*$; else go to 2



Challenge Question 1a

- probability of seeing fleads is $p_h \equiv 0.4$. Another way of understanding value iteration is by reference to the Bellman optimality
- (a)

5. (Challenge Question) A gampler has the opportunity to make bets on the outcomes of This algorithm is called *value iteration*. It can be written as a particularly simple update a sequence of coin flips. If the coin comes up heads, she wins as many dollars as she has staked on that flip; if it is tails, she loses her stake. The game ends when the gambler wins by reaching her goal $\mathbb{E}[R$100, \mathbb{W}(\mathbb{S})$ by trunking dut of money. On each flip, the gambler must decide what portion of her capital to stake, in integer numbers of dollars. This problem can be formulated as an undiscounted, episodic, finite MDP. The state is the gambler's capital, $s \in \{1, 2, ..., 99\}$ and the actions are stakes, $a \in \{0, 1, ..., \min(s, 100 - s)\}$. The rewalls is \$ 1F whethitreaching the sequence (\$4) gap be zero to an verse to an striction. The

What does the value of a state mean in this problem? For example, in a gridworld where optimality equation into an update rule. Also note how the value iteration update is the value of 1 per step, the value represents the expected number of steps to goal. What does then value of astates meanting they game ling's problem relationship bout the painting and maximum plassibles values saude think about a the sale of the state of 99 (Wigirle 3s4n(value) 95) ation). These two are the natural backup operations for computing





Modify the pseudocode for value iteration to more efficiently solve this specific problem, (b) by exploiting your knowledge of the dynamics. *Hint: Not all states transition to every* other state. For example, can you transition from state 1 to state 99?

Value Iteration, for estimating $\pi \approx \pi_*$

Initialize V(s), for all $s \in S^+$, arbitrarily except that V(terminal) = 0Loop: $\Delta \leftarrow 0$ Loop for each $s \in S$: $v \leftarrow V(s)$ $V(s) \leftarrow \max_{a} \sum_{s',r} p(s',r|s,a) \left[r + \gamma V(s') \right]$ $\Delta \leftarrow \max(\Delta, |v - V(s)|)$ until $\Delta < \theta$ Output a deterministic policy, $\pi \approx \pi_*$, such that $\pi(s) = \operatorname{arg\,max}_{a} \sum_{s',r} p(s',r|s,a) \left[r + \gamma V(s') \right]$

Algorithm parameter: a small threshold $\theta > 0$ determining accuracy of estimation

